

# UNIT IV

## Knowledge



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# Propositional logic



- **Propositional Logic (PL)** is a branch of logic that focuses on **statements (propositions)** that can be **either true or false**. It is also known as **Boolean logic** since the truth values are binary—either **True (1)** or **False (0)**.
- In AI, propositional logic forms the **foundation for logical reasoning**, allowing systems to represent **facts** and **rules** about a problem domain. These rules help the system infer new information or make decisions based on the given inputs.
- Propositional logic simplifies **knowledge representation** by breaking down reasoning into **atomic statements** or **propositions**. For example, an AI system used in home automation might have propositions such as:
  - P: “The light is on.”
  - Q: “The window is open.”
- Using **logical connectives**, the system can combine these propositions to represent more complex statements like:
  - “If the light is on and the window is open, turn off the light.”
- By using propositional logic, AI systems can **reason** effectively and perform tasks like **automated decision-making, knowledge representation, and game playing**.

# Basic Facts About Propositional Logic



## 1. Propositions are Declarative Statements:

- In **propositional logic**, each statement, known as a **proposition**, is either **True** or **False**.  
Example:

**P:** “It is raining.” (True or False)

**Q:** “The heater is on.” (True or False)

## 2. Atomic Propositions:

- These are **simple, indivisible statements** that cannot be broken down further. Each atomic proposition represents a basic fact or condition.  
Example: “The door is closed.”

## 3. Compound Propositions:

- **Multiple atomic propositions** can be combined using **logical connectives** (like AND, OR, NOT) to create **compound propositions**.  
Example: “The door is closed AND the heater is on.”

# Basic Facts About Propositional Logic



## 4. Binary Truth Values:

- Every proposition has a **binary truth value**: it can only be **True (1)** or **False (0)**. There are no intermediate states. This simplicity makes propositional logic ideal for **clear-cut decisions**.

## 5. Logical Connectives Combine Propositions:

- Logical connectives such as **AND**, **OR**, **NOT**, **IF-THEN**, and **IF AND ONLY IF** allow us to create more complex propositions from simple ones.

# Syntax of Propositional Logic



- The **syntax** of propositional logic defines the **rules for creating valid propositions**.
  - In propositional logic, we combine **atomic propositions** using **logical connectives** to form more complex statements, known as **compound propositions**.
  - **Building Blocks of Propositional Logic Syntax**
1. **Atomic Propositions:**
- These are basic statements that represent individual facts or conditions.  
Example:
  - **P:** "It is raining."
  - **Q:** "The heater is on."



# Syntax of Propositional Logic



## 2. Logical Connectives:

- Connectives are used to combine atomic propositions to form **compound propositions**.
- **AND** (  $\wedge$  ): True if both propositions are true.
- **OR** (  $\vee$  ): True if at least one proposition is true.
- **NOT** (  $\neg$  ): Negates the truth value of a proposition.
- **IF-THEN** (  $\rightarrow$  ): True unless the first proposition is true and the second is false.
- **IF AND ONLY IF** (  $\leftrightarrow$  ): True if both propositions have the same truth value.

## 3. Compound Propositions:

- These are **more complex statements** formed by connecting atomic propositions using logical connectives.

# Syntax of Propositional Logic



- Example:

“If it is raining and the heater is on, then the room will be warm.”

This can be written in **propositional logic syntax** as:  $(P \wedge Q) \rightarrow R$

Where:

- **P**: “It is raining.”
- **Q**: “The heater is on.”
- **R**: “The room is warm.”



# Syntax of Propositional Logic



- **Example of Propositional Logic**

Let's explore a **real-world scenario** where propositional logic is applied in AI. Consider a **home automation system** that needs to decide whether to **turn on the air conditioner** based on the weather conditions and indoor temperature.

**Scenario:**

- **P:** "It is hot outside."                      **Q:** "The windows are open."                      **R:** "Turn on the air conditioner."

Using **propositional logic**, we can represent the system's decision-making with the following compound proposition:

$$(P \wedge \neg Q) \rightarrow R$$

This logic reads as:

"If it is hot outside **AND** the windows are not open, then **turn on the air conditioner.**"

# Logical Connectives in Propositional Logic



Logical connectives are essential operators that combine **atomic propositions** to form **compound propositions**. These connectives allow AI systems to build more complex rules and perform logical reasoning.

- **AND (  $\wedge$  ):**

- The result is **True** only if both propositions are true.

Example: If **P** is “It is hot” and **Q** is “The fan is on”, then  $(P \wedge Q)$  means both conditions are satisfied.

- **OR (  $\vee$  ):**

- The result is **True** if at least one of the propositions is true.

Example:  $(P \vee Q)$  will be true if either it is hot or the fan is on.

# Logical Connectives in Propositional Logic



- **NOT (  $\neg$  ):**
  - This **inverts** the truth value of the proposition.  
Example: If **P** is true,  $\neg P$  will be false.
- **IF-THEN (  $\rightarrow$  ):**
  - This implies that if the first proposition is true, the second must also be true for the compound statement to be true.  
Example: “If it rains, then the ground will be wet” ( $P \rightarrow Q$ ).
- **IF AND ONLY IF (  $\leftrightarrow$  ):**
  - This is true only when both propositions have the **same truth value** (either both true or both false).  
Example: “It is cloudy if and only if it will rain” ( $P \leftrightarrow Q$ ).

# Precedence of Connectives in Propositional Logic



P	Q	$\neg P$	$P \wedge Q$	$P \vee Q$	$P \rightarrow Q$	$P \leftrightarrow Q$
false	false	true	false	false	true	true
false	true	true	false	true	true	false
true	false	false	false	true	false	false
true	true	false	true	true	true	true

# Precedence of Connectives in Propositional Logic



- When evaluating **compound propositions** with multiple logical connectives, it's important to follow a specific **order of precedence** to ensure accurate results. Similar to arithmetic operations, **logical operators** are evaluated in a defined sequence, from highest to lowest precedence.

## Order of Precedence

1. **NOT (  $\neg$  )** – Negation has the **highest precedence** and is evaluated first.
2. **AND (  $\wedge$  )** – Conjunction is evaluated next, after negations are resolved.
3. **OR (  $\vee$  )** – Disjunction comes after AND operations.
4. **IF-THEN (  $\rightarrow$  )** – Implication is evaluated after OR.
5. **IF AND ONLY IF (  $\leftrightarrow$  )** – Biconditional has the **lowest precedence**.

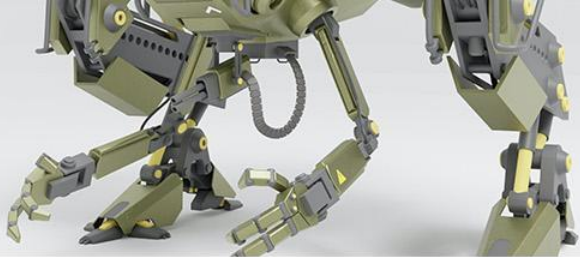
## Logical Equivalence in Propositional Logic



- **Logical equivalence** occurs when two or more logical expressions produce the **same truth values** for all possible combinations of their propositions.
- In other words, two statements are logically equivalent if they always have the **same result**, regardless of the truth values of the individual propositions.
- Two propositions P and Q are logically equivalent if:

$$P \equiv Q$$

# Logical Equivalence in Propositional Logic



## Example of Logical Equivalence

### 1. De Morgan's Laws:

- These laws show how **negations of conjunctions** and **disjunctions** behave:

$$\neg(P \wedge Q) \equiv (\neg P \vee \neg Q)$$

$$\neg(P \vee Q) \equiv (\neg P \wedge \neg Q)$$

### 2. Double Negation:

- Negating a negation gives the original proposition:

$$\neg(\neg P) \equiv P$$

### 3. Implication and Disjunction:

- An implication can be rewritten as:

$$P \rightarrow Q \equiv \neg P \vee Q$$



# Logical Equivalence in Propositional Logic



## Tautologies and Contradictions:

- **Tautology:** A tautology is a statement that is **always true**, no matter the truth values of its individual propositions.
  - **Example:**  $P \vee \neg P \equiv \text{True}$
- **Contradiction:** A contradiction is a statement that is **always false**.
  - **Example:**  $P \wedge \neg P \equiv \text{False}$

# Applications of Propositional Logic in AI



## 1. Knowledge Representation in Expert Systems:

- Represents **rules and facts** to solve domain-specific problems (e.g., medical diagnosis systems).

## 2. Reasoning and Decision-Making:

- AI agents use logical rules to make **decisions** (e.g., robot vacuum cleaners deciding when to start cleaning).

## 3. Natural Language Processing (NLP):

- Helps analyze text and respond logically (e.g., chatbots understanding weather-related queries).

## 4. Game-Playing AI:

- Uses logic to **make strategic moves** (e.g., deciding checkmate in chess).

# Limitations of Propositional Logic



## 1. Inability to Handle Complex Relationships

- Propositional logic cannot represent **relationships between multiple objects** or deal with hierarchies of information.

## 2. No Handling of Uncertainty

- It works only with **true or false** values and cannot deal with **probabilities or uncertain outcomes**, limiting its use in real-world applications involving incomplete data.

## 3. Limited Expressiveness

- It cannot represent **time-based sequences** or dynamic events, which are crucial in some AI systems like speech recognition and robotics.

## 4. Scalability Issues

- As the number of propositions grows, the **complexity of expressions** increases, making reasoning slower and harder to manage.

# First-Order Logic in Artificial intelligence



- In propositional logic, we can only represent the facts, which are either true or false.
- PL is not sufficient to represent the complex sentences or natural language statements.
- The propositional logic has very limited expressive power.
- Consider the following sentence, which we cannot represent using PL logic.

**"Some humans are intelligent", or**

**"Sachin likes cricket."**

To represent the above statements, PL logic is not sufficient, so we required some more powerful logic, such as first-order logic.

# First-Order Logic in Artificial intelligence



- First-order logic is another way of knowledge representation in artificial intelligence. It is an extension to propositional logic.
- FOL is sufficiently expressive to represent the natural language statements in a concise way.
- First-order logic is also known as **Predicate logic or First-order predicate logic**. First-order logic is a powerful language that develops information about the objects in a more easy way and can also express the relationship between those objects.

# First-Order Logic in Artificial intelligence



First-order logic (like natural language) does not only assume that the world contains facts like propositional logic but also assumes the following things in the world:

- **Objects:** A, B, people, numbers, colors, wars, theories, squares, pits, wumpus, .....
- **Relations:** It can be **unary relation such as:** red, round, is adjacent, **or n-any relation such as:** the sister of, brother of, has color, comes between
- **Function:** Father of, best friend, third inning of, end of, .....

As a natural language, first-order logic also has two main parts:

1. **Syntax**
2. **Semantics**

# First-Order Logic in Artificial intelligence



## Syntax of First-Order logic:

- The syntax of FOL determines which collection of symbols is a logical expression in first-order logic. The basic syntactic elements of first-order logic are symbols. We write statements in short-hand notation in FOL.

## Basic Elements of First-order logic:

Following are the basic elements of FOL syntax:

Constant	1, 2, A, John, Mumbai, cat,....
Variables	x, y, z, a, b,....
Predicates	Brother, Father, >,....
Function	sqrt, LeftLegOf, ....
Connectives	$\wedge$ , $\vee$ , $\neg$ , $\Rightarrow$ , $\Leftrightarrow$
Equality	$=$
Quantifier	$\forall$ , $\exists$



# First-Order Logic in Artificial intelligence



## Atomic sentences:

- Atomic sentences are the most basic sentences of first-order logic. These sentences are formed from a predicate symbol followed by a parenthesis with a sequence of terms.
- We can represent atomic sentences as **Predicate (term1, term2, ....., term n)**.

**Example: Ravi and Ajay are brothers:  $\Rightarrow$  Brothers(Ravi, Ajay).**

**Chinky is a cat:  $\Rightarrow$  cat (Chinky).**

# First-Order Logic in Artificial intelligence



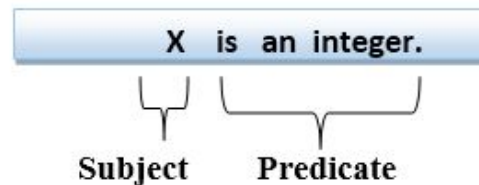
## Complex Sentences:

- Complex sentences are made by combining atomic sentences using connectives.

## First-order logic statements can be divided into two parts:

- **Subject:** Subject is the main part of the statement.
- **Predicate:** A predicate can be defined as a relation, which binds two atoms together in a statement.

**Consider the statement: "x is an integer."** it consists of two parts, the first part x is the subject of the statement and second part "is an integer," is known as a predicate.



# First-Order Logic in Artificial intelligence



## Quantifiers in First-order logic:

- A quantifier is a language element which generates quantification, and quantification specifies the quantity of specimen in the universe of discourse.
- These are the symbols that permit to determine or identify the range and scope of the variable in the logical expression. There are two types of quantifier:
  1. **Universal Quantifier, (for all, everyone, everything)**
  2. **Existential quantifier, (for some, at least one).**

# First-Order Logic in Artificial intelligence



## Universal Quantifier:

- Universal quantifier is a symbol of logical representation, which specifies that the statement within its range is true for everything or every instance of a particular thing.
- The Universal quantifier is represented by a symbol  $\forall$ , which resembles an inverted A.
- **Note: In universal quantifier we use implication " $\rightarrow$ ".**

If  $x$  is a variable, then  $\forall x$  is read as:

- **For all  $x$**
- **For each  $x$**
- **For every  $x$ .**

# First-Order Logic in Artificial intelligence



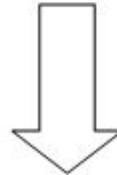
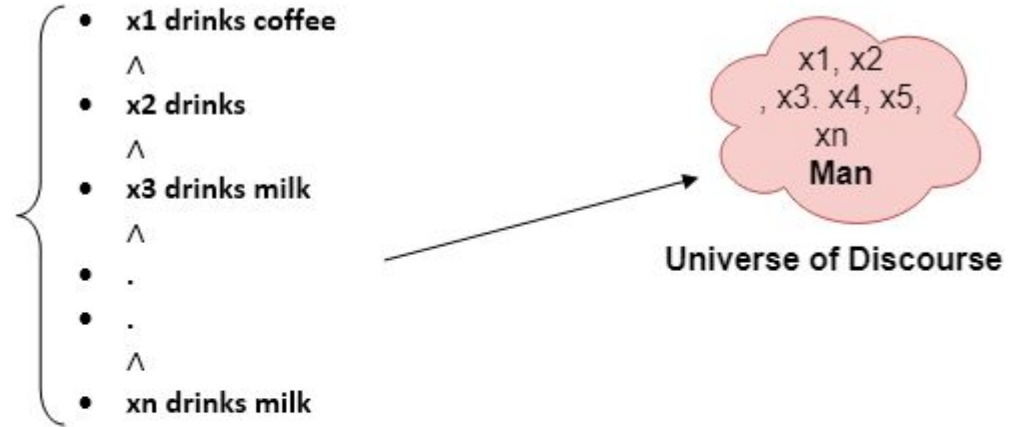
**Example:**

**All man drink coffee.**

Let a variable  $x$  which refers to a man  
so all  $x$  can be represented in  
UOD as below:

$\forall x \text{ man}(x) \rightarrow \text{drink}(x, \text{coffee}).$

It will be read as: There are all  $x$   
where  $x$  is a man who drink coffee.



So in shorthand notation, we can write it as :

# First-Order Logic in Artificial intelligence



## Existential Quantifier:

- Existential quantifiers are the type of quantifiers, which express that the statement within its scope is true for at least one instance of something.
- It is denoted by the logical operator  $\exists$ , which resembles as inverted E. When it is used with a predicate variable then it is called as an existential quantifier.

**Note:** In Existential quantifier we always use **AND** or **Conjunction** symbol ( $\wedge$ ).

If  $x$  is a variable, then existential quantifier will be  $\exists x$  or  $\exists (x)$ . And it will be read as:

- **There exists a 'x.'**
- **For some 'x.'**
- **For at least one 'x.'**

# First-Order Logic in Artificial intelligence



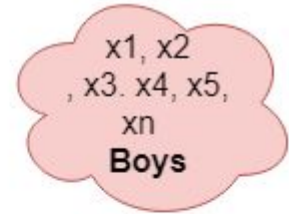
## Example:

Some boys are intelligent.

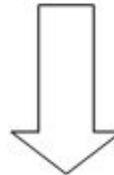
- $x_1$  is intelligent
- $\vee$
- $x_2$  is intelligent
- $\vee$
- $x_3$  is intelligent
- $\vee$
- .
- .
- $\vee$
- $x_n$  is intelligent

$\exists x: \text{boys}(x) \wedge \text{intelligent}(x)$

It will be read as: There are some  
 $x$  where  $x$  is a boy who is intelligent.



Universe of Discourse



So in short-hand notation, we can write it as:



# First-Order Logic in Artificial intelligence



## Points to remember:

- The main connective for universal quantifier  $\forall$  is implication  $\rightarrow$ .
- The main connective for existential quantifier  $\exists$  is and  $\wedge$ .

## Properties of Quantifiers:

- In universal quantifier,  $\forall x \forall y$  is similar to  $\forall y \forall x$ .
- In Existential quantifier,  $\exists x \exists y$  is similar to  $\exists y \exists x$ .
- $\exists x \forall y$  is not similar to  $\forall y \exists x$ .

# First-Order Logic in Artificial intelligence



Some Examples of FOL using quantifier:

## 1. All birds fly.

In this question the predicate is "**fly(bird).**"

And since there are all birds who fly so it will be represented as follows.

$$\forall x \text{ bird}(x) \rightarrow \text{fly}(x).$$

## 2. Every man respects his parent.

In this question, the predicate is "**respect(x, y),**" where **x=man,** and **y= parent.**

Since there is every man so will use  $\forall$ , and it will be represented as follows:

$$\forall x \text{ man}(x) \rightarrow \text{respects}(x, \text{parent}).$$

# First-Order Logic in Artificial intelligence



## 3. Some boys play cricket.

In this question, the predicate is "**play(x, y)**," where x= boys, and y= game. Since there are some boys so we will use  $\exists$ , and it will be represented as:

$$\exists x \text{ boys}(x) \rightarrow \text{play}(x, \text{cricket}).$$

## 4. Not all students like both Mathematics and Science.

In this question, the predicate is "**like(x, y)**," where x= student, and y= subject. Since there are not all students, so we will use  $\forall$  with negation, so following representation for this:

$$\neg \forall (x) [ \text{student}(x) \rightarrow \text{like}(x, \text{Mathematics}) \wedge \text{like}(x, \text{Science}) ].$$

# First-Order Logic in Artificial intelligence



## 5. Only one student failed in Mathematics.

In this question, the predicate is "**failed(x, y),**" where **x= student,** and **y= subject.**

Since there is only one student who failed in Mathematics, so we will use following representation for this:

$$\exists (x) [ \text{student}(x) \rightarrow \text{failed} (x, \text{Mathematics}) \wedge \forall (y) [\neg(x==y) \wedge \text{student}(y) \rightarrow \neg\text{failed} (x, \text{Mathematics})].$$

# First-Order Logic in Artificial intelligence



## Free and Bound Variables:

The quantifiers interact with variables which appear in a suitable way. There are two types of variables in First-order logic which are given below:

**Free Variable:** A variable is said to be a free variable in a formula if it occurs outside the scope of the quantifier.

**Example:**  $\forall x \exists (y)[P(x, y, z)]$ , where  $z$  is a free variable.

**Bound Variable:** A variable is said to be a bound variable in a formula if it occurs within the scope of the quantifier.

**Example:**  $\forall x [A(x) B(y)]$ , here  $x$  and  $y$  are the bound variables.

# Resolution in FOL



- Resolution is a theorem proving technique that proceeds by building refutation proofs, i.e., proofs by contradictions.
- Resolution is used, if there are various statements are given, and we need to prove a conclusion of those statements. Unification is a key concept in proofs by resolutions. Resolution is a single inference rule which can efficiently operate on the **conjunctive normal form or clausal form**.
- Resolution is used, if there are various statements are given, and we need to prove a conclusion of those statements. Unification is a key concept in proofs by resolutions. Resolution is a single inference rule which can efficiently operate on the **conjunctive normal form or clausal form**.

# Resolution in FOL

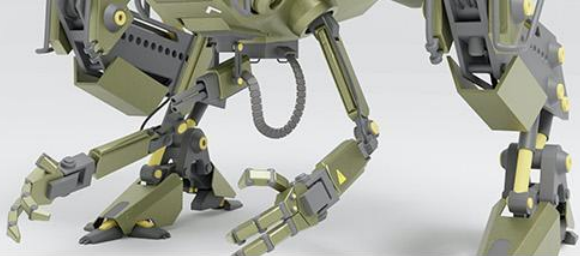


## Steps for Resolution:

1. Conversion of facts into first-order logic.
2. Convert FOL statements into CNF
3. Negate the statement which needs to prove (proof by contradiction)
4. Draw resolution graph (unification).



# Resolution in FOL



## Convert FOL statements into CNF

### 1. Eliminate biconditionals and implications:

- Eliminate  $\Leftrightarrow$ , replacing  $\alpha \Leftrightarrow \beta$  with  $(\alpha \Rightarrow \beta) \wedge (\beta \Rightarrow \alpha)$ .
- Eliminate  $\Rightarrow$ , replacing  $\alpha \Rightarrow \beta$  with  $\neg\alpha \vee \beta$ .

### 2. Move $\neg$ inwards:

- $\neg(\forall x p) \equiv \exists x \neg p$ ,
- $\neg(\exists x p) \equiv \forall x \neg p$ ,
- $\neg(\alpha \vee \beta) \equiv \neg\alpha \wedge \neg\beta$ ,
- $\neg(\alpha \wedge \beta) \equiv \neg\alpha \vee \neg\beta$ ,
- $\neg\neg\alpha \equiv \alpha$

# Resolution in FOL



**3. Standardize variables apart by renaming them: each quantifier should use a different variable.**

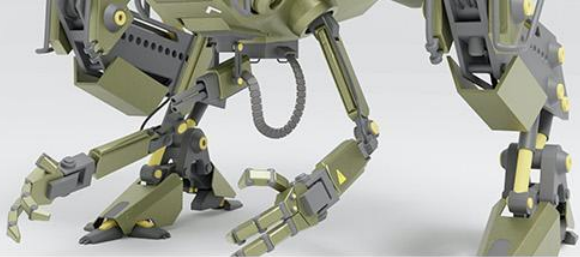
**4. Skolemize:** each existential variable is replaced by a Skolem constant or Skolem function of the enclosing universally quantified variables.

- For instance,  $\exists x \text{ Rich}(x)$  becomes  $\text{Rich}(G1)$  where  $G1$  is a new Skolem constant.

**5. Drop universal quantifiers**

- For instance,  $\forall x \text{ Person}(x)$  becomes  $\text{Person}(x)$ .

# Resolution in FOL



## Example:

- John likes all kind of food.
- Apple and vegetable are food.
- Anything anyone eats and not killed is food.
- Anil eats peanuts and still alive.
- Harry eats everything that Anil eats.
- **John likes peanuts.**

# Resolution in FOL



## Step-1: Conversion of Facts into FOL

In the first step we will convert all the given statements into its first order logic.

- a.  $\forall x: \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$
  - b.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
  - c.  $\forall x \forall y: \text{eats}(x, y) \wedge \neg \text{killed}(x) \rightarrow \text{food}(y)$
  - d.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$ .
  - e.  $\forall x : \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$
  - f.  $\forall x: \neg \text{killed}(x) \rightarrow \text{alive}(x)$
  - g.  $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$
  - h.  $\text{likes}(\text{John}, \text{Peanuts})$
- } **added predicates.**

# Resolution in FOL



## Step-2: Conversion of FOL into CNF

In First order logic resolution, it is required to convert the FOL into CNF as CNF form makes easier for resolution proofs.

### 2.1 Eliminate all implication ( $\rightarrow$ ) and rewrite

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  $\forall x \forall y \neg [\text{eats}(x, y) \wedge \neg \text{killed}(x)] \vee \text{food}(y)$
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
6.  $\forall x \neg [\neg \text{killed}(x)] \vee \text{alive}(x)$
7.  $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$

# Resolution in FOL



## Step-2: Conversion of FOL into CNF

### 2.1 Eliminate all implication ( $\rightarrow$ ) and rewrite

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  **$\forall x \forall y \neg [\text{eats}(x, y) \wedge \neg \text{killed}(x)] \vee \text{food}(y)$**
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
6.  **$\forall x \neg [\neg \text{killed}(x)] \vee \text{alive}(x)$**
7.  $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$
8.  $\text{likes}(\text{John}, \text{Peanuts}).$

### 2.2 Move negation ( $\neg$ ) inwards and rewrite

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  $\forall x \forall y \neg \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y)$
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
6.  $\forall x \text{killed}(x) \vee \text{alive}(x)$
7.  $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$
8.  $\text{likes}(\text{John}, \text{Peanuts}).$

# Resolution in FOL



## Step-2: Conversion of FOL into CNF

### 2.2 Move negation ( $\neg$ ) inwards and rewrite

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  $\forall x \forall y \neg \text{eats}(x, y) \vee \text{killed}(x) \vee \text{food}(y)$
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall x \neg \text{eats}(\text{Anil}, x) \vee \text{eats}(\text{Harry}, x)$
6.  $\forall x \text{killed}(x) \vee \text{alive}(x)$
7.  $\forall x \neg \text{alive}(x) \vee \neg \text{killed}(x)$
8.  $\text{likes}(\text{John}, \text{Peanuts}).$

### 2.3 Rename variables or standardize variables

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  $\forall y \forall z \neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall w \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
6.  $\forall g \text{killed}(g) \vee \text{alive}(g)$
7.  $\forall k \neg \text{alive}(k) \vee \neg \text{killed}(k)$
8.  $\text{likes}(\text{John}, \text{Peanuts}).$

# Resolution in FOL



## Step-2: Conversion of FOL into CNF

### 2.3 Rename variables or standardize variables

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  $\forall y \forall z \neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall w \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
6.  $\forall g \text{ killed}(g) \supset \vee \text{alive}(g)$
7.  $\forall k \neg \text{alive}(k) \vee \neg \text{killed}(k)$
8.  $\text{likes}(\text{John}, \text{Peanuts}).$

### 2.4 Eliminate existential instantiation quantifier by elimination.

In this step, we will eliminate existential quantifier  $\exists$ , and this process is known as **Skolemization**. But in this example problem since there is no existential quantifier so all the statements will remain same in this step.



# Resolution in FOL



## Step-2: Conversion of FOL into CNF

### 2.3 Rename variables or standardize variables

1.  $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple}) \wedge \text{food}(\text{vegetables})$
3.  $\forall y \forall z \neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
4.  $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
5.  $\forall w \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
6.  $\forall g \text{killed}(g) \supset \vee \text{alive}(g)$
7.  $\forall k \neg \text{alive}(k) \vee \neg \text{killed}(k)$
8.  $\text{likes}(\text{John}, \text{Peanuts}).$

### 2.5 Drop Universal quantifiers.

In this step we will drop all universal quantifier since all the statements are not implicitly quantified so we don't need it.

1.  $\neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple})$
3.  $\text{food}(\text{vegetables})$
4.  $\neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
5.  $\text{eats}(\text{Anil}, \text{Peanuts})$
6.  $\text{alive}(\text{Anil})$
7.  $\neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
8.  $\text{killed}(g) \vee \text{alive}(g)$
9.  $\neg \text{alive}(k) \vee \neg \text{killed}(k)$
10.  $\text{likes}(\text{John}, \text{Peanuts}).$

# Resolution in FOL



## Step-3: Negate the statement to be proved

In this statement, we will apply negation to the conclusion statements, which will be written as  $\neg \text{likes}(\text{John}, \text{Peanuts})$

## Step-4: Draw Resolution graph:

Now in this step, we will solve the problem by resolution tree using substitution. For the above problem, it will be given as follows:

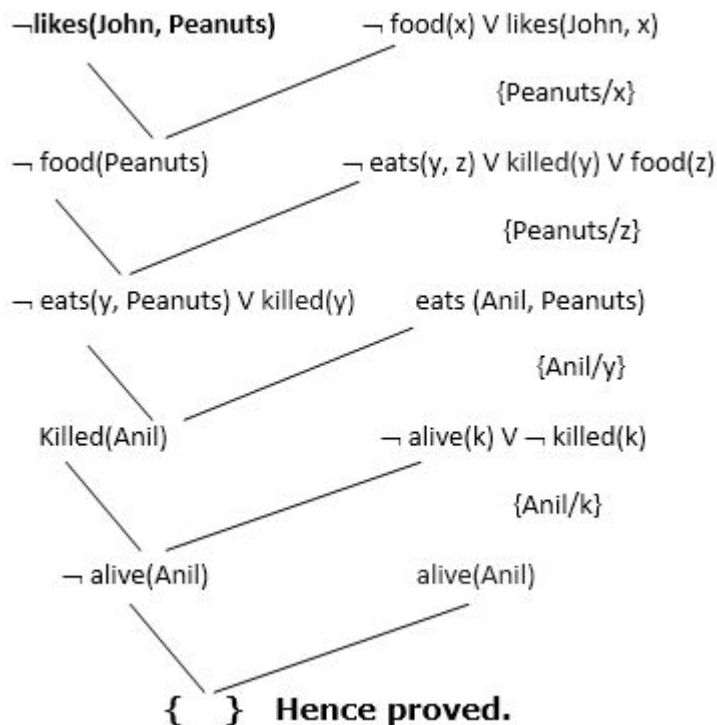
# Resolution in FOL



## Step-4: Draw Resolution graph:

Now in this step, we will solve the problem by resolution tree using substitution. For the above problem, it will be given as follows:

1.  $\neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
2.  $\text{food}(\text{Apple})$
3.  $\text{food}(\text{vegetables})$
4.  $\neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$
5.  $\text{eats}(\text{Anil}, \text{Peanuts})$
6.  $\text{alive}(\text{Anil})$
7.  $\neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
8.  $\text{killed}(g) \vee \text{alive}(g)$
9.  $\neg \text{alive}(k) \vee \neg \text{killed}(k)$
10.  $\text{likes}(\text{John}, \text{Peanuts})$ .



# Resolution in FOL



Hence the negation of the conclusion has been proved as a complete contradiction with the given set of statements.